

groups

$$\begin{pmatrix} a & \tau a(1-a) \\ \tau a(1-a) & 1-a \end{pmatrix}$$

$$e_1 = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}$$

$$e_2 = \begin{pmatrix} \tau & \sqrt{1-\tau} \\ \sqrt{1-\tau} & 1-\tau \end{pmatrix}$$

$$e_3 = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}$$

$$e_4 = \begin{pmatrix} \tau & 0 & \sqrt{1-\tau} & 0 & 0 \\ 0 & \tau & 0 & \sqrt{1-\tau} & 0 \\ \sqrt{1-\tau} & 0 & 1-\tau & 0 & 0 \\ 0 & \sqrt{1-\tau} & 0 & 1-\tau & 0 \\ 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$e_5 = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\frac{\tau}{1-\tau} = \frac{t}{1+t+t^2}$$

$$\frac{1-2\tau}{1-\tau} = \frac{1+t^2}{(1+t+t^2)}$$

$e_1 e_2 = \tau e_1$ ✓
 $e_2 e_1 = (1-\tau) e_2$ ✓
 $e_3 e_4 = \tau e_3$ ✓
 $e_4 e_3 = (1-\tau) e_4$ ✓
 $e_5 e_i = 0$
 $e_i e_5 = 0$

$$1-2\tau = \frac{1+t^2}{(1+t)^2}$$

$$1-\tau = \frac{1+t+t^2}{(1+t)^2}$$

$$g_1 = \begin{pmatrix} t & 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 & 0 \\ 0 & 0 & t & 0 & 0 \\ 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 & -1 \end{pmatrix}$$

$$g_2 = \frac{1}{(1+t)} \begin{pmatrix} -1 & \alpha & 0 & 0 & 0 \\ \alpha & t^2 & 0 & 0 & 0 \\ 0 & 0 & -1 & \alpha & 0 \\ 0 & 0 & \alpha & t^2 & 0 \\ 0 & 0 & 0 & 0 & -(1+t) \end{pmatrix}$$

$$\alpha = \sqrt{t(1+t+t^2)}$$

$$\beta = \sqrt{t(1+t^2)}$$

$$g_3 = \begin{pmatrix} t & 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{1+t+t^2} & \frac{(t+1)\beta}{1+t+t^2} \\ 0 & 0 & 0 & \frac{(t+1)\beta}{1+t+t^2} & \frac{t^3}{1+t+t^2} \end{pmatrix}$$

$$g_4 = \frac{1}{1+t} \begin{pmatrix} -1 & 0 & \alpha & 0 & 0 \\ 0 & -1 & 0 & \alpha & 0 \\ \alpha & 0 & t^2 & 0 & 0 \\ 0 & \alpha & 0 & t^2 & 0 \\ 0 & 0 & 0 & 0 & -(1+t) \end{pmatrix}$$

$$g_5 = \begin{pmatrix} t & 0 & 0 & 0 & 0 \\ 0 & t & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 & -1 \end{pmatrix}$$

so $g_5 \in \langle g_1, g_2, g_3 \rangle$

all multiplied by $(-t^{-\frac{2}{5}})$